

! Keywords: Inventory / Lot Sizing / Marketing / Product Management / Production / Reorder Point / Scheduling / Uncertainty;

! Two Product Capacitated Lot-sizing Problem.

! $Y_{it} = 1$ if product i is produced in period t ,

! $X_{Ast} = 1$ if demands in periods s through t are

! satisfied from production in period s , for product A ,

! $X_{Bst} = 1$ etc. for product B .

MIN 100 YA1 + 100 YA2 + 150 YA3 + 150 YA4 + 200 YA5
+ 200 YA6 + 30 YB1 + 40 YB2 + 30 YB3 + 55 YB4
+ 45 YB5 + 45 YB6 + 200 XA11 + 560 XA12 + 1260 XA13
+ 1620 XA14 + 2720 XA15 + 5520 XA16 + 360 XA22
+ 1060 XA23 + 1420 XA24 + 2520 XA25 + 5320 XA26
+ 700 XA33 + 1060 XA34 + 2160 XA35 + 4960 XA36
+ 320 XA44 + 1320 XA45 + 3920 XA46 + 900 XA55
+ 3300 XA56 + 2000 XA66 + 40 XB11 + 160 XB12
+ 360 XB13 + 540 XB14 + 740 XB15 + 1055 XB16
+ 120 XB22 + 320 XB23 + 500 XB24 + 700 XB25
+ 1015 XB26 + 160 XB33 + 310 XB34 + 485 XB35
+ 765 XB36 + 150 XB44 + 325 XB45 + 605 XB46
+ 125 XB55 + 335 XB56 + 175 XB66

subject to

! For product A:

! If a production lot was depleted in period $i-1$ (the $-$ terms),

! then a production run of some sort must be started in

! period i (the $+$ terms)

A1) $XA11 + XA12 + XA13 + XA14 + XA15 + XA16 = 1$

A2) $-XA11 + XA22 + XA23 + XA24 + XA25 + XA26 = 0$

A3) $-XA12 - XA22 + XA33 + XA34 + XA35 + XA36 = 0$

A4) $-XA13 - XA23 - XA33 + XA44 + XA45 + XA46 = 0$

A5) $-XA14 - XA24 - XA34 - XA44 + XA55 + XA56 = 0$

A6) $-XA15 - XA25 - XA35 - XA45 - XA55 + XA66 = 0$

! The setup forcing constraints for A

FA1) $YA1 - XA11 - XA12 - XA13 - XA14 - XA15 - XA16 \geq 0$

FA2) $YA2 - XA22 - XA23 - XA24 - XA25 - XA26 \geq 0$

FA3) $YA3 - XA33 - XA34 - XA35 - XA36 \geq 0$

FA4) $YA4 - XA44 - XA45 - XA46 \geq 0$

FA5) $YA5 - XA55 - XA56 \geq 0$

FA6) $YA6 - XA66 \geq 0$

! Same constraints for product B:

B1) $+XB11 + XB12 + XB13 + XB14 + XB15 + XB16 = +1$

B2) $-XB11 + XB22 + XB23 + XB24 + XB25 + XB26 = 0$

B3) $-XB12 - XB22 + XB33 + XB34 + XB35 + XB36 = 0$

B4) $-XB13 - XB23 - XB33 + XB44 + XB45 + XB46 = 0$

B5) $-XB14 - XB24 - XB34 - XB44 + XB55 + XB56 = 0$

B6) $-XB15 - XB25 - XB35 - XB45 - XB55 + XB66 = 0$

! The setup forcing constraints;

FB1) $YB1 - XB11 - XB12 - XB13 - XB14 - XB15 - XB16 \geq 0$

FB2) $YB2 - XB22 - XB23 - XB24 - XB25 - XB26 \geq 0$

FB3) $YB3 - XB33 - XB34 - XB35 - XB36 \geq 0$

FB4) $YB4 - XB44 - XB45 - XB46 \geq 0$

FB5) $YB5 - XB55 - XB56 \geq 0$

FB6) $YB6 - XB66 \geq 0$

! Here are the capacity constraints for each period;

! The coefficient of a variable is the associated lotsize;

CAP1) $40 XA11 + 100 XA12 + 200 XA13 + 240 XA14$
 $+ 340 XA15 + 540 XA16 + 20 XB11 + 50 XB12$
 $+ 90 XB13 + 120 XB14 + 145 XB15 + 180 XB16$
 ≤ 200

CAP2) $60 XA22 + 160 XA23 + 200 XA24 + 300 XA25$
 $+ 500 XA26 + 30 XB22 + 70 XB23 + 100 XB24$
 $+ 125 XB25 + 160 XB26 \leq 200$

CAP3) $100 XA33 + 140 XA34 + 240 XA35 + 440 XA36$
 $+ 40 XB33 + 70 XB34 + 95 XB35 + 130 XB36 \leq 200$

CAP4) $40 XA44 + 140 XA45 + 340 XA46 + 30 XB44$
 $+ 55 XB45 + 90 XB46 \leq 200$

CAP5) $100 XA55 + 300 XA56 + 25 XB55 + 60 XB56$
 ≤ 200

CAP6) $200 XA66 + 35 XB66 \leq 200$

END
INTEGER 12